Effect of mixed surface terminations on the structural and electrochemical properties of two-dimensional $Ti_3C_2T_2$ and V_2CT_2 MXenes multilayers

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MXenes, a family of layered transition metal carbides and nitrides, have shown great promise for use in emerging electrochemical energy storage devices, including batteries and supercapacitors. MXene surfaces are terminated by mixed -O, -F and -OH functional groups as a result of the chemical etching production process. These functional groups are known to be randomly distributed over the surfaces, with limited experimental control over their composition. There is considerable debate regarding the contribution of these functional groups to the properties of the underlying MXene material. For instance, their measured Li or Na capacity is far lower than that predicted by theoretical simulations, which generally assume uniformly terminated surfaces. The extent to which this structural simplification contributes to such discrepancies is unknown. We address this issue by employing first-principles calculations to compare the structural, electronic and electrochemical properties of two common MXenes, namely $Ti_3C_2T_2$ and V_2CT_2 , with both uniform terminating groups and explicitly mixed terminations. Weighted averages of uniformly-terminated layer properties are found to give excellent approximations to those of more realistic, mixed termination structures. This approximation holds for the lattice parameters, the electronic density of states and the work function. The sodium storage capacity and volume change during sodiation in the interlayer space of these MXenes with mixed surface terminations are also investigated. The redox reaction is shown to be confined to the terminating groups for low concentrations of intercalated Na, with the oxidation state of the metal atoms unaffected until higher concentrations of intercalated Na are achieved. Finally, the average open circuit voltage is shown to be very similar for both $Ti_3C_2T_2Na$ and V_2CT_2Na with mixed terminations, although it is highly sensitive to the particular composition of the terminating groups.

I. INTRODUCTION

Li-ion batteries (LIBs) currently dominate the highperformance electrochemical storage market, but limited Li resources mean that alternatives are being explored. Sodium-ion batteries (NIBs), in particular, could present a viable and cost effective replacement for LIBs due to the natural abundance and low-cost of sodium. Na has a similar redox potential to Li and exhibits similar intercalation chemistry. Unfortunately, current electrode materials for Li-ion batteries, such as graphite, show little electroactivity for NIBs,¹ necessitating the development of alternative electrodes.

In this regard, the family of MXene materials show promise. MXenes are layered materials produced from their parent $M_{n+1}AX_n$ phases through a selective chemical etching of the covalently bonded A layer (M is an early transition metal, A is typically aluminum, X is C and/or N and n = 1 - 3). Ti₃C₂ was the first MXene material to be experimentally produced, etched from its parent Ti₃AlC₂ phase using a hydrofluoric-acid treatment.² Since then, at least 19 different MXene compositions have been synthesized with many more predicted to be stable.³

Hydrophilic, conductive, layered MXenes show promising electroactivity for Li-, Na-, and K-ions.^{4,5} V₂C has a Li⁺ capacity of 280 mAhg⁻¹ at 1C and 125 mAhg⁻¹ at 10C cycling rates.⁶ Ti₃C₂ has a Na⁺ capacity of 100 mAhg⁻¹ over 100 cycles⁷ and an initial K⁺ capacity of 260 mAhg⁻¹ which is reduced to 45 mAhg⁻¹ after 120 cycles.⁸ For comparison, conventional graphite cells for Li-ion batteries have a maximum specific capacity of 372 mAhg^{-1} , but are currently operating close to their theoretical limit and cannot handle high cycling rates.⁹ Given the number of MXene materials which remain to be investigated, there is considerable scope for improvement.

One means of improving the electrochemical behaviour of MXene materials is to tune their surface chemistry. As a consequence of the chemical etching process, the surfaces of MXene layers are generally covered by mixed termination groups, predominately -O, -F and -OH, collectively designated T_x . These terminating groups are known to be randomly distributed over the surface with limited experimental control over their composition. $^{10-12}$ Theoretical investigations into these materials generally make a significant simplification: they assume the MXene surface is covered by uniform terminations of -O, -F or -OH groups, rather than the mixed terminations found experimentally. They find that the specific terminations have a significant effect on the structural, electronic and electrochemical behaviour of MXene layers.^{13–15} As a result, there are large discrepancies between the calculated and experimental properties of these materials, particularly for quantities such as their capacity.

In this work, first-principles density-functional theory (DFT) calculations are used to determine how the structural, electronic and electrochemical properties of two of the most popular members of the MXene family, namely $Ti_3C_2T_x$ and V_2CT_x , depend on the nature of the terminating groups. In the following, we restrict x to be 2, i.e., $Ti_3C_2T_2$ and V_2CT_2 , so that only full coverage of terminating groups on the surface is considered. Given both the computational expense of modelling mixed surface terminations and the inability of the uniformly terminated structures to reproduce experimental results, we propose that a better approximation can be made by taking the weighted average of the properties of the uniformly terminated materials. This would allow much cheaper calculations as uniformly terminated structures require a smaller unit cell. Given the difficulties in achieving uniform terminations experimentally. we also discuss how some of the properties predicted for these structures are affected by mixed termination populations, particularly the ultra-low work function predicted for -OH terminated MXene layers. Furthermore, we investigate Na-ion intercalation and the charge storage mechanism of these structures with mixed terminations and show how sensitive the open circuit voltage is to the mixed terminations.

This paper is organized as follows: Section II discusses the model for mixed terminations while under the restriction of periodic boundary conditions as well as the choice of termination composition. Section III A and Section III B show how the structural and electronic properties of both monolayer and multilayer $Ti_3C_2T_2$ and V_2CT_2 MXenes differ from those which assume uniform terminations and compare the results to available experimental data. Finally, section III C discusses the intercalation of Na into these layers.

II. THEORETICAL METHODS

A. Modelling mixed terminations

In order to model the effect of mixed terminations on a MXene layer, we randomly populate the surface sites of a 3×3 supercell of Ti₃C₂ and V₂C with -O, -F and -OH groups such that, when averaged over nine different supercells, they reproduce a typical ratio of surface terminations found experimentally. For Ti₃C₂T₂, the terminating atoms are placed at the hollow sites directly above the central Ti atom, while for V₂CT₂, the terminating atoms are placed directly above the V atom on the opposite surface. This is in agreement with previous calculations.^{11,16} Note that each layer has 18 possible binding sites -9 on each surface. A full structural relaxation is then performed.

The bulk stacked structure is modelled by randomly combining two of these monolayers in an AB-stacking configuration, as shown in Fig. 1. A further full structural relaxation is performed on these stacked layers to determine the interlayer spacing. Four different stacked structures are considered and their properties are averaged.

We define a simple weighted average of the properties of the three uniformly covered MXenes as:



FIG. 1. (color online) Typical examples of stacked $Ti_3C_2T_2$ (left) and V_2CT_2 (right) multilayers with mixed terminations and an AB-stacking configuration. The high percentage of -OH (-F) groups in such a typical mixed $Ti_3C_2T_2$ (V_2CT_2) structure is evident.

$$\bar{P} = \frac{x}{2}P_{-\rm O} + \frac{y}{2}P_{-\rm F} + \frac{z}{2}P_{-\rm OH}$$
(1)

The properties considered include, for example, the lattice constants, the density of states and the work functions. P_{-T} refers to the value of the property associated with the uniformly terminated structures, and x, y and z are related to the populations of the -O, -F and -OH groups on the surface, respectively (c.f. Table I).

B. Termination composition

Experiment has shown conclusively that the ratio of terminating groups on the surface of MXene layers depends critically on the details of the chemical etching process. Using a 10% concentration of hydrofluoric acid (HF) to etch Ti₃AlC₂ resulted in ordered crystalline layers with AB-stacking and a stoichiometric formula of $Ti_3C_2O_{0.13}F_{0.83}(OH)_{1.04}$.¹⁷ This composition is modelled in the results presented here. (Given the limited number of structures which we can work with, our model reproduces this as $Ti_3C_2O_{0.11}F_{0.864}(OH)_{1.025}$.) Etching the same MAX phase material with NH_4HF_2 produced layered $Ti_3C_{1.8}O_{2.3}F_{0.2}$.¹⁸ There is less experimental information available about the distribution and relative populations of terminating groups on V_2CT_x layers. To reflect the higher concentration of -F groups generally found in V_2CT_x compared to $Ti_3C_2T_x$ as reported by experiment,^{6,19} we employ an average composition of $V_2CO_{0.42}(OH)_{0.4}F_{1.19}$ in the calculations presented here. The chosen surface terminations of both materials are summarized in Table I. Note that the populations given in Table I are the target populations, and correspond to the average of the nine structures considered (18 surfaces). The individual surfaces are populated probabilistically according to these statistics, but there is a variance in the populations of -O, -F and -OH groups between the 18 individual surfaces.

	\boldsymbol{x}	\boldsymbol{y}	\boldsymbol{z}
$\mathrm{Ti}_{3}\mathrm{C}_{2}\mathrm{O}_{x}\mathrm{F}_{y}(\mathrm{OH})_{z}$	0.11~(6%)	0.86~(43%)	1.03~(51%)
$V_2 CO_x F_y (OH)_z$	0.42~(21%)	1.19~(59%)	0.40~(20%)

TABLE I. The composition of terminating groups in $Ti_3C_2T_2$ and V_2CT_2 as used in this work. They were chosen to reflect typical experimental values. The percentage contribution of each terminating group to the total is also given.

C. Density Functional Theory

Density functional theory calculations are performed using the VASP code.^{20–22} The Perdew-Burke-Ernzerhof $(PBE)^{23}$ parametrization of the generalized gradient approximation (GGA) is employed. The plane wave basis set is converged using an 800 eV energy cutoff. Structural relaxations of the monolaver supercell are carried out using a $3 \times 3 \times 1$ k-point Monkhorst-Pack mesh²⁴ to sample the three-dimensional Brillouin zone, while the stacked layer supercell is relaxed using a $3 \times 3 \times 2$ k-point mesh. The electronic structure is then calculated using a $15 \times 15 \times 1$ and $8 \times 8 \times 4$ mesh for the monolayers and stacked layers, respectively. Dispersion forces are included using the semi-empirical approach of Grimme (DFT-D3).^{25,26} For calculations involving monolayers, a vacuum layer of at least 25 Å is included in the direction normal to the surface to electronically decouple neighboring slabs and the dipole correction is applied.^{27,28} The work function, $\Phi = eV_{\text{vacuum}} - E_{\text{F}}$, is obtained by calculating the planar average of the electrostatic potential across the super-cell and taking the vacuum potential, V_{vacuum} , sufficiently far from the surface along the surface normal direction.

III. RESULTS & DISCUSSION

A. Monolayers

1. Structural Properties

The in-plane lattice constants of $Ti_3C_2T_2$ and V_2CT_2 monolayers are given in Table II. The results presented for the uniformly terminated monolayers are in good agreement with previous calculations in the literature,^{29–31} showing that the –O terminated structures have the smallest in-plane lattice constant while the –OH terminated structures have the largest lattice constant. This is true for both $Ti_3C_2T_2$ and V_2CT_2 .

The average in-plane lattice constant of the nine different $Ti_3C_2T_2$ monolayers with mixed terminations is 9.24 Å, with individual structures having values ranging between 9.22 Å and 9.27 Å. Notably, this averaged value is identical to \bar{a} , the value achieved by taking a weighted average of the lattice constant of the three uniformly terminated monolayers (c.f. Eqn. 1). These values are in

TABLE II. In-plane lattice parameters, in Å, of monolayer $Ti_3C_2T_2$ and V_2CT_2 , including those structures with uniformly terminated -O, -F and -OH groups, the lattice constants given by taking a weighted average of the lattice constants of the uniformly covered surfaces, calculated according to Eqn. 1 and the average in-plane lattice constant of 9 different structures with mixed terminations (according to the compositions given in Table I). In all cases, the lattice constant is given for a 3×3 unit cell.

good agreement with an experimentally reported value of 9.17 Å.³² The average in-plane lattice constant of V₂CT₂ structures with mixed terminations is 8.84 Å, and individual structures have values ranging between 8.79 Å and 8.87 Å. This averaged value is within 0.6% of that found by taking the weighted average of lattice constants of the the uniformly terminated structures, 8.89 Å.

It is clear that taking a simple weighted average of the uniformly terminated in-plane lattice constants gives excellent agreement with those determined by explicitly considering mixed terminations. We now consider if this approximation is also applicable to the electronic properties of these monolayers.

2. Electronic Properties

The total density of states (DOS) calculated for Ti_3C_2 and V_2C monolayers with uniform terminations are shown in Fig. 2(a) and (c), respectively. They are in good agreement with previous calculations.^{33,34} Fig. 2(b) and (d) then compare the averaged DOS of the structures with mixed terminations (solid black line) with those calculated as a weighted average of the uniformly terminated structures, shown with a red dotted line.

First, we note that in all cases, and for both $Ti_3C_2T_2$ and V_2CT_2 , the monolayers are found to be metallic, in agreement with experiment.^{34,35} Second, the DOS of the monolayers with mixed terminations is in excellent agreement with that calculated as a weighted average in a wide energy range between -4 eV and +2 eV (-2 eVand +2 eV) for $Ti_3C_2T_2$ (V_2CT_2). The origin of this agreement lies in the identity of the states located around the Fermi level of both materials. This can be seen by considering the density of states projected onto the relevant atomic orbitals, shown in Fig. 2(e) and (f). The density of states of $Ti_3C_2T_2$ between -4 eV and +2 eVis predominately comprised of contributions from Ti and C. For V_2CT_2 , contributions from V and C dominate in the energy region between -2 eV and +2 eV. States associated with the terminating groups are located lower in energy.

As a result, in the energy window where states from the MXene layer, rather than the terminating atoms, dominate, the density of states of the structures with mixed terminations can be reproduced by a weighted average, as shown in Fig. 2(b) and (d). For energies outside this region, the detailed agreement is not as good, suggesting that the exact contribution of the terminating groups cannot be determined by a weighted average of the individual components. The origin of this behaviour is related to the mutual interactions between the terminating groups. For example, the large peak in the DOS of V_2CF_2 at -4.2 eV (c.f. Fig. 2(c)), which due to a hybridization between F, C and V states, is not present in the DOS of the structures with mixed terminations, despite their high concentration (59% of the total terminations).

3. Work Function

It has been predicted that MXene monolayers which are uniformly terminated with -OH groups will have an ultra-low work function of 1.85 eV, allowing them to function as very efficient field emitters.³⁶ However, given the difficulties associated with experimentally controlling the surface terminations of these materials, and the intimate relationship between a material's work function and the particulars of its surface, it is not clear that this ultralow work function can be realistically achieved. Here, we determine whether the low work-function associated with uniform -OH terminations persists even when other terminating groups are present.

The work functions of the uniformly terminated structures, the average value of the mixed terminated structures as well as the value found by taking a weighted average of the uniformly terminated structures are shown in Fig. 3. The values for the uniformly terminated surfaces are in good agreement with previous calculations.^{36,37} In particular, we find a very high work function for structures with a uniform –O termination and an ultra-low work function for structures terminated with uniform – OH groups. The work functions of –O and –F terminated V_2CT_2 are higher than those of $Ti_3C_2T_2$, by 0.75 eV and 0.58 eV, respectively.

The work function of $Ti_3C_2T_2$ monolayers with mixed terminations is 2.46 eV. Note that this was calculated as the averaged work function of 18 different surfaces. Individual surfaces had work functions ranging between 1.44 eV and 3.68 eV. For the V₂CT₂ monolayers with mixed terminations, the average work function is 4.64 eV, with the work functions of individual surfaces ranging between 2.5 eV and 5.6 eV.

The general trend is clear: $Ti_3C_2T_2$, which has a high percentage of terminating -OH groups (51%), has a lower work-function than V_2CT_2 which is dominated by -F



FIG. 2. Total density of states calculated for (a) uniformly terminated Ti_3C_2 monolayers, (b) $Ti_3C_2T_2$ monolayers with mixed terminations (black solid line) and a weighted average of the uniformly terminated monolayers (red dashed line), (c) uniformly terminated V₂C monolayers, (d) V₂CT₂ monolayers with with mixed terminations (black solid line) and a weighted average of the uniformly terminated V₂C monolayers (red dashed line). The gray shaded area in (b) and (d) show the population standard deviation of the individual structures with mixed terminations. The total projected density of states of (e) Ti_3CT_2 monolayers with mixed terminations and (f) V₂CT₂ monolayers with mixed terminations.

groups (59%). However, taking a simple weighted average of work functions of uniformly terminated structures results in a large error, particularly for $Ti_3C_2T_2$.

To probe this further, Fig. 4 compares the calculated work function of each of the eighteen individual surfaces, Φ , to the value that would be found by taking the weighted average of the uniformly covered surfaces, $\overline{\Phi}$. Note that the composition of each individual surface was taken into account here – it is the averaged composition of these eighteen surfaces that gives the composition reported in Table I. It is clear that $\overline{\Phi}$ always overestimates the actual work function of the Ti₃C₂T₂ surface by approximately 1 eV. On average, this results in an error of 38%. For V₂CT₂, the average error is much smaller, at 9%, although the error of some individual structures



FIG. 3. Work functions of both uniformly and mixed terminated $Ti_3C_2T_2$ (blue bars) and V_2CT_2 (orange bars). The error bars on the work-function calculated for the mixed terminations represent the range of values calculated for each individual structure. Note that the work functions of bare Ti_3C_2 and V_2C monolayers are 3.91 eV and 4.60 eV, respectively.



FIG. 4. The work function calculated for each individual surface, Φ , for Ti₃C₂T₂ (blue circles) and V₂CT₂ (orange squares), compared to the value that would be found by taking the weighted average of the uniformly covered surfaces, $\bar{\Phi}$. The black dashed line corresponds to the case when $\Phi = \bar{\Phi}$, and the gray shaded area shows a region within ±1 eV of this line.

is larger. Agreement tends to improve when structures with high numbers of -OH groups are excluded, even if those groups are located on the opposite surface. Indeed, this is reason for the better agreement for V₂CT₂ which, on average, has only 20% -OH groups on the surface, compared to 51% for Ti₃C₂T₂. Finally, we note that even the maximum value of the Ti₃C₂T₂ work function found in these calculations (3.68 eV at 22% -OH concentration) is significantly lower that the experimentally reported values of 5.28 eV³⁵ or 4.35 eV.³⁸ The composition of the terminating groups in those structures was not reported, however. It is likely that significant quantities of -O groups or H₂O molecules were present on their surfaces.

Fig. 5(a) then shows how the work function of the individual surfaces of $Ti_3C_2T_2$ with mixed terminations depends on the percentage of -OH groups on the surface. We find that approximately 60% -OH groups is sufficient to achieve a work function of between 1.50 eV and 1.85 eV. Similarly, for V_2CT_2 , there is a general trend for the work function to increase as the concentration of -F groups on the surface increases, as shown in Fig. 5(b).



FIG. 5. (a) The work function calculated for each individual $Ti_3C_2T_2$ surface, Φ , as a function of the percentage of -OH groups in that particular structure. (b) The work function calculated for each individual V_2CT_2 surface, Φ , as a function of the percentage of -F groups in that particular structure. Note that for each concentration of -OH or -F groups, the other two termination types are varying randomly - it is for this reason there is a spread of almost 0.5 eV for an -OH concentration of 44.4%.

We can conclude that achieving very fine control over the surface terminations is not necessary in order to tune the work function to its extremal values. The ultra-low work function predicted for a uniform termination of – OH groups can also be achieved with approximately 60% –OH groups. Similarly, work functions above 5 eV can be achieved with approximately 50% –F groups on the surface.

B. Stacked Layers

The chemical etching process used to produced MX ene materials usually results in stacked layers rather than completely delaminated layers.³⁹ The interlayer space can then be intercalated by ions such as Li or Na or even small molecules^{32,40} Here, we discuss the structural and electronic properties of stacked Ti₃C₂T₂ and V₂CT₂ with mixed terminations according to Table I.

1. Structural Properties

The calculated lattice constants of stacked $Ti_3C_2T_2$ and V_2CT_2 are given in Table III. Compared to the monolayers, we find that stacking has only a marginal effect on the in-plane lattice constants, reducing them by no more than 0.9%. This is the case for both uniform and mixed terminations. The agreement between the inplane lattice constant of the mixed termination stacked

	a (Å)	c (Å)
Ti ₃ C ₂ T ₂ Uniform		
- O	9.06	18.72
$-\mathrm{F}$	9.13	18.46
- OH	9.27	19.86
Weighted average	9.20	19.20
$Ti_3C_2T_2$ Mixed	9.16	19.47
$Ti_3C_2T_2$ Experiment ¹⁷	9.147	19.15
V ₂ CT ₂ Uniform		
- O	8.63	13.70
$-\mathrm{F}$	8.90	14.07
- OH	8.96	14.12
Weighted average	8.90	14.07
V_2CT_2 Mixed	8.84	14.07

TABLE III. Structural parameters of stacked $Ti_3C_2T_2$ and V_2CT_2 , with uniform (-O, -OH and -F) and mixed terminations according to the composition given in Table I, for a 3×3 unit cell. The lattice constants found by taking a weighted average of the uniformly terminated values are also given. Note that Ref. 17 has the same composition of terminating groups as considered in this work.

 $Ti_3C_2T_2$ layers and the experimental value for a structure with the same composition is excellent, with values of 9.16 Å and 9.147 Å, respectively.¹⁷

The out-of-plane lattice constant, c, depends sensitively on the nature of the surface terminations. The c lattice constant of Ti₃C₂O₂ is smallest at 18.72 Å, and largest for –OH terminated structures at 19.86 Å. These differ from the experimental value of 19.15 Å by 2.2% and -3.7%, respectively.¹⁷ Considering mixed terminations improves the agreement with experiment, giving a value of 19.47 Å, an overestimation of only 1.7%. Other experimental compositions report values of c ranging between 19.3 Å and 20.89 Å.^{7,32,41–44}

Here again, we find that taking the simple weighted average of the lattice constants of the uniformly terminated $Ti_3C_2T_2$ stacked layers results in excellent agreement with the values found by explicitly considering mixed terminations. The weighted in-plane lattice constant differs from the one calculated with mixed terminations by 0.4%, while the out-of-plane lattice constant differs by 1.4%.

For the case of the V₂CT₂, the *c* lattice constant is also strongly dependent on the composition of the surface terminations. It ranges from 13.70 Å for –O terminations to 14.12 Å for uniform –OH terminations. Due to the prevalence of –F terminations on the surface of the structures with mixed terminations, the *c* value is found to be 14.07 Å, identical to that of a structure with uniform –F terminations. As for $Ti_3C_2T_2$, the in-plane lattice constants determined as a weighted average are in excellent agreement with those determined for the structures with mixed terminations, with differences of 0.7% and 0.0% for the in-plane and out-of-plane lattice constants, respectively.

However, these values - whether uniform or mixed are considerably smaller than any reported experimental c values for V₂CT₂, which range between 19 and 24 Å.^{6,45} This is a considerable difference of 5 – 10 Å and as such cannot be attributed to a difference in the exact composition of the terminating groups. It is more likely that the experimental hypothesis that there are significant quantities of H₂O molecules intercalated between the layers of V₂CT₂ is correct.^{6,19,46} Depending on the etching process, other impurities may also be present which can modify the interlayer distance.⁴⁷

C. Na Intercalation

To gain further insight into the effect of mixed terminations on the intercalation chemistry of these MXene layers, we now consider the structural and electronic changes that occur after Na intercalation in structures with mixed terminating groups. In the following, these intercalated structures are designated $Ti_3C_2T_2Na_x$ and $V_2CT_2Na_x$. A full intercalated Na monolayer corresponds to x = 1, or 9 intercalated Na atoms in the 3×3 unit cell considered here.

Compared to the unintercalated MXene layers, there are two changes to note. The first is related to the stacking. The un-intercalated structure has a Bernal-like ABstacking, as shown in Fig. 1. After Na intercalation, the layers shift to a simple hexagonal stacking, in agreement with experiment.¹¹ In this configuration, the terminating atoms of adjacent layers are located directly opposite one another. Furthermore, ion intercalation typically causes the number of -OH groups on the surface to be reduced or even eliminated.^{8,33,48,49} This instability of the H atoms in –OH terminations is also found to be the case here. As a result, we assume that after Na intercalation, each -OH group is replaced with a -O termination. Finally, in agreement with experiment¹¹ and previous calculations,^{14,33} the Na atoms are located directly on top of the carbon atoms for both $Ti_3C_2T_2$ and V_2CT_2 .

1. Lattice Constants

The structural properties of $Ti_3C_2T_2$ and V_2CT_2 with mixed terminations are shown in Fig. 6 as a function of the number of intercalated Na atoms. For $Ti_3C_2T_2$, we find that the in-plane lattice constant averages 9.09 Å before intercalation for the structure with a ground state Bernal-like stacking and with all hydrogen atoms removed. After Na intercalation, the in-plane lattice constant initially decreases slightly by 0.02 Å until approximately x = 2/9. This agrees Shi et al.,⁴³ who showed experimentally that the in-plane lattice constant decreases after Na intercalation by approximately 0.03 Å (for a 3×3 unit cell). For concentrations greater than x = 5/9, the *a* lattice parameter increases, to reach a maximum value of 9.15 Å for a full intercalated Na monolayer. This corresponds to an average percentage change of 0.7% compared to the unintercalated multilayers. This is in agreement with the overall increase in the in-plane lattice constant with Na intercalation predicted by Eames et al.³¹ and can be attributed to an increase in the lateral electrostatic repulsion between the Na atoms at increasing concentration.

The change in the out-of-plane lattice constant upon Na intercalation is, unsurprisingly, significantly higher. The insertion of a single Na atom increases c by an average value of 1.58 Å, from 18.87 Å to 20.45 Å. The c lattice constant then increases with increasing Na concentration, rising by 0.55 Å at x = 5/9, before decreasing slowly (by 0.2 Å) with further increases in Na, to reach 20.80 Å for a full intercalated monolayer.

V₂CT₂ behaves broadly similarly upon Na intercalation, as shown in Fig. 6(b). The in-plane lattice constant initially decreases by a similar amount to $Ti_3C_2T_2$, but the average maximum increase is slightly larger, at 0.16 Å, corresponding to an increase of 1.8%. In general, the spread of values across the individual mixed termination structures is slightly larger for V_2CT_2 than for $Ti_3C_2T_2$. The out-of-plane lattice constant also behaves similarly to Ti₃C₂T₂ after Na intercalation, especially for low concentrations of Na. There is a 1.60 Å increase in cafter the intercalation of the first Na atom, from 13.7 Å to 15.3 Å. This rises to a maximum increase of 2.18 Å for x = 4/9 before decreasing slowly. This is an almost identical increase compared to the case of $Ti_3C_2T_2$. The c value starts to increase again for a full intercalated Na monolayer.

Given that structural changes during charging and discharging are the primary cause of performance degradation in batteries, small volume changes after the first intercalation are desirable. $Ti_3C_2T_2$ and V_2CT_2 have a maximum volume change of 11% and 16%, respectively, compared to the un-intercalated structure. However, some experiments have reported that Na does not always completely deintercalate from the MXene material, even at high voltages, i.e., it behaves as a pillar holding the interlayer distance $open^{7,42}$ with further changes in the c lattice constant restricted to ± 0.4 Å. We find the change in the c lattice value reduces to 2.8% and 4.2%, for $Ti_3C_2T_2Na_x$ and $V_2CT_2Na_x$, respectively, if we assume that after the first sodiation the interlayer spacing is held open by a single Na atom. These changes correspond to a change of ± 0.6 Å for both Ti₃C₂T₂Na_x and $V_2CT_2Na_x$, in excellent agreement with experiment.

2. Comparison to Experiment

A comparison between these lattice changes and the experimentally reported values should be performed care-



FIG. 6. Changes in the lattice parameters of a 3×3 supercell of stacked (a) Ti₃C₂T₂Na_x and (b) V₂CT₂Na_x as a function of the concentration of Na atoms, x. The solid lines are averages over 4 configurations with mixed terminations which have individual values that range between the shaded areas.

fully. Firstly, as stated previously, the composition of the terminating groups will affect the lattice constants, so that MXene created using different acids or different concentrations of acids will likely yield different changes in the lattice parameter. For example, Lukatskaya et al. found that increases in the c lattice constant depend sensitively on the type of salt used in the electrolyte. They showed that the c value of $Ti_3C_2T_x$ increased by as much as 5.0 Å in high-pH solutions such as Na_2CO_3 , while neutral solutions such as the sulphates only increased c by approximately 0.7 Å.⁴² As such, the results presented here will only be valid for the stated composition of terminating groups. That being said, the spread of values indicated by the shaded regions in Fig. 6 show how sensitive changes in the lattice parameter induced by Na intercalation are to changes in the terminating groups.

Secondly, several experiments have reported the existence of a Na double layer intercalated between the layers.^{11,50} To determine if this is the case, we calculate the effects of intercalating a Na double layer in Ti₃C₂T₂ and V₂CT₂ for a limited number of structures. For both Ti₃C₂T₂Na₂ and V₂CT₂Na₂, the *c* lattice constant increases by 7.97 Å compared to the unintercalated case. The vertical distance between the two Na layers is 3.1 Å, which is similar to that calculated for a Na bilayer adsorbed on a Ti₃C₂O₂ monolayer (3.08Å).³³ The average vertical distance between the Na atoms and the terminating atoms is 1.5 Å, while the average distance between Na and the carbon atoms is 3.93 Å. The increase in the c lattice parameter found here for a Na double layer in V_2CT_2 is considerably higher than the experimentally reported increase of 4.6 Å,⁵⁰ suggesting that this value does not indicate the presence of a Na double layer, but rather other intercalants such as H₂O, or a large solvation shell around the intercalated Na atoms.

3. Co-intercalated water

As previously mentioned, many experimental structures also have considerable quantities of H₂O or other co-intercalants located between the MXene layers.⁵¹ In many cases, drying the material in vacuum results in a reduction in the c lattice parameter found initially, as the water is evicted. Kajiyama et al.⁷ show the c lattice parameter of $Ti_3C_2T_x$ to increase from 19.4 Å to 25 Å upon first sodiation. However, after drying the material, the c value decreases to 21.8 Å, which is in much better agreement with the theoretical value of 20.80 Å found here. Similarly, Osti et al.⁴¹ reports two peaks in the Xray diffraction pattern of Na intercalated $Ti_3C_2T_x$, corresponding to c lattice constants of 23.98 Å and 21.22 Å. The smaller of these two values is in good agreement with our theoretical value, while the former could indicate the presence of co-intercalants.

While a thorough investigation of the effects of water co-intercalation on the structural properties of these materials is beyond the scope of this work, an initial indication of its effect can be found by the introduction a single H_2O molecule into the $Ti_3C_2T_2Na_{5/9}$ and $V_2CT_2Na_{5/9}$ structures. For the case of $Ti_3C_2T_2Na_{5/9}$, we find that the c lattice constant increases by 0.29 Å, from 20.99 Å to 21.28 Å. For $V_2CT_2Na_{5/9}$, the lattice constant increases by 0.5 Å, from 15.81 Å to 16.32 Å. The larger increase found for V_2CT_2 compared to $Ti_3C_2T_2$ for the same concentration of co-intercalated water could be responsible for the unexpectedly large c lattice constant of V_2CT_2 .^{6,19,46} In both cases, the introduction of H_2O causes Na atoms to move away from their high-symmetry adsorption position. This would agree with the experimental work of Shi et al. who report that the intercalated Na atoms are disordered and do not sit at well defined locations.⁴³

4. Electronic Properties

The total density of states of stacked, mixed terminated $Ti_3C_2T_2$ and V_2CT_2 are shown in Fig. 7 for increasing concentrations of intercalated Na. For each value of Na concentration, the DOS was averaged over the four considered mixed termination structures. By comparing to Fig. 2(e) and (f), we can see that Na intercalation results in the states associated with the -F groups being moved to lower energies by approximately 1.3 eV in both materials. For the case of $Ti_3C_2T_2Na_1$, this results in a gap of 0.7 eV opening between these F states and those associated with O and Ti. The states associated with O are also moved to lower energies by approximately 0.5 eV for a full intercalated Na monolayer compared to the unintercalated case in both materials.



FIG. 7. Total density of states of (a) $Ti_3C_2T_2Na_x$ and (b) $V_2CT_2Na_x$ as a function of Na intercalation, ranging from the clean stacked MXene (x = 0 dark blue) to $Ti_3C_2T_2Na$ ($(3 \times 3)x = 9$, dark red).

To determine the effect of Na intercalation on the charge distribution, we calculated the change in charge density that occurs after intercalation. This charge density difference (CDD) is shown in Fig. 8 (a) and (b) for the intercalation of a single Na atom and a full Na monolayer, respectively, into the interlayer space of $Ti_3C_2T_2$ for a particular mixed termination. In both cases, there is a reduction of charge density around the Na atom. Bader charge analysis⁵² finds that, regardless of the concentration, the Na atom loses 0.8e, which is transferred to the MXene layer. For a single intercalated Na atom, this charge is predominantly located on the terminating groups nearest it. For the case shown here, the closest O atom gains approximately 0.09e, while the F atom gains 0.03e. Considerably less charge is transferred to the Ti atoms (0.03e is transferred to the Ti closest to the Na atom) and there is no charge transferred at all to the carbon atoms. For the case of a full intercalated Na monolayer, there is a large increase in the amount of charge transferred to the two extremal Ti layers. Each Ti gains 0.11e, so that their oxidation value rises from 2.35e to 2.46e. In contrast, the internal Ti layer and the C atoms gain very little excess charge (0.02e). The accumulation of charge on the terminating O atoms rises to 0.34e while the F atoms now gain 0.13e. This is in agreement with the experimental work of Kajiyama et al. who find a much larger change in the oxidation state of the terminating groups compared to the Ti atoms during sodiation/desodiation.⁷ Furthermore, Lukatskaya et al. find that the oxidation state of the Ti atoms rises from 2.33e to 2.43e (i.e., by 0.1e per Ti atom) over a 0.7V window,⁵³ which is in excellent agreement with the results presented here.

A very similar picture emerges for Na intercalation into V_2CT_2 , as shown in Fig. 8 (c) and (d) for a single intercalating Na atom and a full Na monolayer, respectively. For the case of a single inserted Na atom, 0.8e is redistributed from the Na atom to the neighboring terminating atoms of the MXene layer. For a full intercalated Na monolayer, 0.8e from each of the Na atoms is again distributed to the O atoms (0.36e) and to the F atoms (0.16e). The V atoms gain 0.11e, so that their oxidation state rises from 3.52e to 3.63e. Bak et al.⁴⁵ report that the electrochemical redox reaction mainly takes place at the vanadium sites during the sodiation process, with an average change in the vanadium oxidation state of 0.2e.



FIG. 8. Slices of charge density difference after sodiation, shown in a plane perpendicular to the MXene layers and through the center of the 3×3 unit cell for Ti₃C₂T₂Na_x, where (a) x = 1/9, (b) x = 1, and V₂CT₂Na_x, where (c) x = 1/9, (d) x = 1. Here, red and blue colors indicate accumulation and depletion of charge density, respectively. The scale is in units of a.u.⁻³.

5. Open Circuit Voltage and Specific Capacity

The voltage delivered by a rechargeable battery is a key quantity to determine the effectiveness of a novel electrode material. Assuming the following half-cell reaction vs Na/Na⁺:

$$\mathrm{Ti}_{3}\mathrm{C}_{2}\mathrm{T}_{2} + x\mathrm{Na}^{+} + xe^{+} \longleftrightarrow \mathrm{Ti}_{3}\mathrm{C}_{2}\mathrm{T}_{2}\mathrm{Na}_{x}$$

and neglecting volume and entropy effects, the open circuit voltage (OCV) can be approximated as: 54

$$OCV \approx -\frac{E_f}{x} = -\frac{1}{x} [E_{MXene+xNa} - E_{MXene} - xE_{Na}]$$
(2)

where E_f is the formation energy of sodiation, x is the number of Na atoms intercalated between the layers of the stacked MXene structure and E_{Na} is the energy of metallic Na in its bulk body centered cubic structure.



FIG. 9. OCV as a function of the number of intercalated Na atoms, x, in $Ti_3C_2T_2Na_x$ (blue circles) and $V_2CT_2Na_x$ (orange squares). The solid line is an average over 4 different termination configurations which have values that range between the shaded areas.

The OCV is shown in Fig. 9 for both $Ti_3C_2T_2Na_x$ and $V_2CT_2Na_x$ with mixed terminations and for increasing concentrations of intercalated Na. The OCV is positive over the entire range of Na concentrations considered and for both $Ti_3C_2T_2$ and V_2CT_2 . While the OCV of V_2CT_2 is higher by almost 0.4 eV at the lowest concentration of Na considered, the difference between the two materials decreases approximately linearly with increasing Na concentration to 0.05 eV. At this point, x = 1, the OCV of both materials is approximately 1.7 eV. In both cases, the OCV reaches a maximum at a Na concentration of x = 1/3. The shaded regions in Fig. 9 indicates how sensitive the OCV is to the details of the individual termination configurations. For the case of $Ti_3C_2T_2$, the OCV varies over an average range of approximately 0.39 eV, while for V_2CT_2 the range is larger, at 0.54 eV.

Given that the OCV is related to the formation energy, the positive value at x = 1 indicates that a full intercalated Na monolayer does not correspond to maximum capacity. We find the OCV associated with a Na double layer remains positive at 0.71 eV for Ti₃C₂T₂Na₂ and 0.78 eV for V₂CT₂Na₂. While this would suggest that the concentration of intercalated Na atoms can be greater than even two monolayers, the experimentally reported capacity suggests that this is not achieved in practice. The theoretical specific capacity is defined, in units of $mAhg^{-1}$, as:

$$C_t = \frac{xzF}{3.6\left[M_{\text{electrode}} + xM_{\text{Na}}\right]},$$

where x is the number of intercalated atoms, z is the valance state of the intercalated atoms, in this case 1, F is Faraday's constant, $M_{\rm electrode}$ is the molar mass of the electrode material and $M_{\rm Na}$ is the molar mass of a Na atom.



FIG. 10. Theoretical specific capacity of stacked $Ti_3C_2T_2Na_x$ and $V_2CT_2Na_x$ using the molar mass of the structures with mixed terminations according to Table I.

The calculated specific capacities of $Ti_3C_2T_2Na_x$ and $V_2CT_2Na_x$, are shown in Fig. 10. For the case of a full intercalated monolayer, the theoretical specific capacity of stacked $Ti_3C_2T_2Na_1$ is 119 mAhg⁻¹, whereas it is 155 mAhg⁻¹ for the case of stacked $V_2CT_2Na_1$. Note here that the exact make-up of the terminating groups contributes relatively little to the total specific capacity, given the dominance of the molar weight of Ti and V to the total. The specific capacity of $Ti_3C_2T_2$ and V_2CT_2 with a double layer of sodium atoms is 216 mAhg⁻¹ and 274 mAhg⁻¹, respectively. The higher specific capacity of V_2CT_2 is as a result of its smaller molar mass compared to $Ti_3C_2T_2$.

Xie et al. report a first cycle discharge capacity of 370 mAhg^{-1} for $\text{Ti}_3\text{C}_2\text{T}_x$. The initial charge capacity is smaller at 164 mAhg}^{-1}. By 10 cycles the capacity has reduced to 100 mAhg}^{-1} and finally to 80 mAhg}^{-1} at 120 cycles.⁸ Kajiyama et al. find a first sodiation capacity of 270 mAhg⁻¹, reducing to 100 mAhg⁻¹ at 100 cycles.⁷ While such high capacities for the first sodiation may suggest a very high intercalation concentration, this is not supported by structural data. Instead, such high capacities may be as a result of side reactions including the formation of a solid-electrolyte interphase (SEI) or electrolyte decomposition. A capacity of approximately 100 mAhg^{-1} would correspond to a Na concentration of x = 0.9. Bak et al. report an experimental capacity of 200 mAhg^{-1} during the first sodiation discharge in V_2CT_x , and a capacity of 125 mAhg⁻¹ for the first charge. This is reduced to 90 mAhg⁻¹ after the first few cycles.⁴⁵ Similarly, Dall'Agnese et al.⁵⁰ report an specific capacity of approximately 70 mAh/g at low scanning rates for V_2CT_x . This would correspond to a Na concentration of x = 0.44 - 0.55 in V₂CT₂Na_x. Many factors

can result in the experimental capacity being lower that the predicted value, including solvation effects, the presence of solvated ions or other impurities, and the presence of any residue of the precursor ternary carbide material.

IV. CONCLUSION

We have examined how mixed termination groups affect the structural, electronic and electrochemical properties of $Ti_3C_2T_2$ and V_2CT_2 . Several structures with mixed terminations were considered such that their average reflected a typical experimental composition. We show that while these individual structures show the properties to be quite sensitive to the particular terminating groups, the average value is generally in very good agreement with experiment.

Furthermore, in cases where taking mixed terminations into account explicitly is unfeasible due to the computational expense, a significantly improved approximation can be achieved by taking a suitable weighted average of uniformly-terminated layers. This procedure was shown to yield accurate results for the lattice parameters, the electronic density of states and the work function of these materials.

Interestingly, we highlight that some of the highly desirable properties postulated for uniformly terminated surface are not highly sensitive to the exact surface termination. For example, the ultra-low work functions proposed for uniformly –OH terminated MXenes can be achieved with only 60% –OH groups on the surface. Such a result demonstrates that, despite the experimental difficulties in controlling the surface terminations of these MXene materials, they remain highly promising for technological applications.

Finally, the sodium storage capacity and structural changes during sodiation were also investigated for the mixed terminated $Ti_3C_2T_2$ and V_2CT_2 structures. The redox reaction was found to be confined to the terminating groups at low concentrations of intercalated Na, with the oxidation state of the metal atoms unaffected until a higher Na concentration is achieved, in excellent agreement with experiment. The open circuit voltage is shown to be highly sensitive to the particular composition of the terminating groups, varying by approximately 0.4 eV at each Na concentration.

CONFLICTS OF INTEREST

There are no conflicts to declare.

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